# Temperature dependent study of thermophysical and optical properties of binary mixtures of imidazolium based ionic liquids 

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#### Abstract

The experimental values of densities $(\rho)$ and speeds of sound $(u)$ of the binary mixtures of ionic liquid 1-butyl-3-methylimidazolium tetrafluoroborate $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]$ with $\alpha, \omega$-propanediols have been used to calculate the internal pressure $\left(\pi_{i}\right)$, free volume $\left(V_{f}\right)$, excess internal pressure ( $\pi_{i}^{\mathrm{E}}$ ), excess free volume ( $V_{\mathrm{f}}^{\mathrm{E}}$ ), excess free energy ( $G^{\mathrm{E}}$ ), excess enthalpy ( $H^{\mathrm{E}}$ ) and excess entropy ( $T_{5}{ }^{\mathrm{E}}$ ) covering the entire composition range expressed by mole fractions of ionic liquid at temperatures ( $298.15,303.15,308.15,313,15,318.15$ and 323.15 K ). The refractive indices ( $n_{\mathrm{D}}$ ) of these mixtures have been measured at above-mentioned temperatures and the deviations in refractive index ( $\Delta_{\phi}{ }^{n} \mathrm{D}$ ) have been calculated. The results have been interpreted in terms of intermolecular interactions between the component molecules in the mixture. The variations of these excess properties with composition indicate that the interactions between $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]$ and $\alpha, \omega$-propanediols in these mixtures follows the order: 1,2-propanediol > 1,3-propanediol.


Keywords: Thermodynamic properties, Excess thermodynamic properties, Refractive index, Molecular interactions, Alkanediols, 1-Butyl-3-methylimidazolium tetrafluoroborate

The present investigation comprises a part of our ongoing research program on the properties of binary mixtures containing ionic liquids involved in separation units for recovering industrial solvents, food engineering, or pharmacological applications ${ }^{1-5}$. The study of propagation of ultrasonic waves in liquids and liquid mixtures is of immense significance for examining the nature of intermolecular and intramolecular interactions in these systems. The ultrasonic speed measurements coupled with other experimental data such as density and refractive index have been used to calculate various thermophysical parameters such as compressibility, internal pressure, free volume, free energy, enthalpy, entropy and their excess values ${ }^{6-8}$. These parameters play a vital role in understanding of the molecular interactions in binary mixtures.

In the present study, the binary mixtures of the imidazolium based ionic liquid, 1-butyl-3methylimidazolium tetrafluoroborate $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]$ with 1,2-propanediol and 1,3-propanediol have been investigated. The interest in ionic liquids was initiated
because of advantageous physicochemical properties such as negligible vapour pressure, high thermal and electrochemical stability, high solvating power, etc. ${ }^{9,10}$. In the recent years ionic liquids have been used in various applications such as organic synthesis, catalysis, electrochemical devices and solvent extraction for different compounds ${ }^{1}$, separation technology ${ }^{2,3}$, homogeneous catalysis ${ }^{4}$, and templates for zeolites ${ }^{5}$. Ionic liquids have also been used as an effective material to evaluate the reaction rate in hydrogenation ${ }^{11}$, hydroformylation ${ }^{12}$ and carbonylation ${ }^{13}$ processes. Glycols find widespread application in automotive, aviation, explosive, textile, surface coating, and food, cosmetic, pharmaceutical, tobacco, petroleum, and other industries ${ }^{14-16}$. The $\alpha, \omega$-propanediols contain both proton donor as well as proton acceptor groups, therefore, there exists a significant degree self-association through inter- and intra-molecular hydrogen bonding in pure state. The thermophysical behavior of $\alpha, \omega$-propanediols both as a pure compound or in binary mixtures were studied in recent years ${ }^{17-20}$. Over the years, thermodynamic
functions such as internal pressure, free volume have garnered significant interest from chemists, physicists and chemical engineers, as they provide a measure of explaining molecular interactions, internal structure, clustering phenomenon, ionic interactions and dipolar interactions ${ }^{21-25}$, and hence have been employed subsequently to investigate the intermolecular interactions in binary mixtures.

In the present article, the refractive indices ( $n_{\mathrm{D}}$ ) of 1-butyl-3-methylimidazolium tetrafluoroborate [Bmim $]\left[\mathrm{BF}_{4}\right]+1,2$-propanediol or 1,3-propanediol binary mixtures have been measured over entire composition range, expressed by mole fraction ( $x_{1}$ ) of $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]$ at temperatures 298.15, 303.15, 308.15, $313,15,318.15$ and 323.15 K and at atmospheric pressure. The calculate the internal pressure $\left(\pi_{i}\right)$, free volume $\left(V_{\mathrm{f}}\right)$, excess internal pressure ( $\left.\pi_{i}^{\mathrm{E}}\right)$, excess free volume ( $V_{\mathrm{f}}^{\mathrm{E}}$ ), excess free energy ( $G^{\mathrm{E}}$ ), excess enthalpy ( $H^{\mathrm{E}}$ ) and excess entropy ( $T S^{\mathrm{E}}$ ) and deviations in refractive index ( $\Delta_{\phi} n_{\mathrm{D}}$ ) of mixing of 1-butyl-3-methylimidazolium tetrafluoroborate ([Bmim] [ $\left.\mathrm{BF}_{4}\right]$ ) with 1,2-propanediol or 1,3-propanediol binary mixtures have been calculated from experimental values ultrasonic speeds ( $u$ ) and densities ( $\rho$ ) and refractive index $\left(n_{\mathrm{D}}\right)$. The experimental data of $u$ and $\rho$ of these binary mixtures has been taken from our previous study ${ }^{26}$. The variations of these excess parameters with composition and temperature of the mixtures are discussed in terms of intermolecular interactions in these mixtures.

## Materials and Methods

The ionic liquid, 1-butyl-3-methylimidazolium tetrafluoroborate $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]$ (Iolitec GmbH , Germany; CAS 174899-83-3, purity > 0.99 mass fraction) was purified by vacuum distillation; 1,2-propanediol (Sigma Aldrich, CAS No. 57-55-6, purity $>0.99$ mass fraction) and 1,3- propanediol (Sigma Aldrich, CAS No. 504-63-2, purities > 0.99 mass fraction) were purified by fractional distillation under low pressure. The water content in the ionic liquid and alkanediols was determined using a Karl Fischer Titrator (Metrohm, 890 Titrando) ${ }^{27}$. The water content was found to be less than 40 ppm . The mass fraction purities of the purified chemicals as determined by gas chromatography were: $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]>0.995,1,2$-propanediol $>0.996$ and 1,3 -propanediol $>0.996$. The mixtures were prepared by mass and were kept in special airtight stopper glass
bottles to avoid evaporation. The weighings were done by using an electronic balance (Model: CPA225D, Sartorious, Germany) with a precision of $\pm 0.01 \mathrm{mg}$. The uncertainty in the mole fraction was estimated to be less than $\pm 1 \times 10^{-4}$.

The refractive indices of the samples were measured using an automatic refractometer (Abbemat-HP Dr. Kernchen, Anton Paar, Austria). The refractometer was calibrated by measuring the refractive index of millipore quality water and tetrachloroethylene before each series of measurements. The calibration was further checked with pure liquids of known refractive index values. The uncertainty in the refractive index measurements was within $\pm 0.00005$ and for temperature it was less than $\pm 0.03 \mathrm{~K}$.

## Results and Discussion

## Excess properties

The internal pressure of a fluid is related to the thermal pressure coefficient $(\partial P / \partial T)_{V}$ by the following well-known thermodynamic equation of state,
$\pi_{\mathrm{i}}=\left(\frac{\partial E}{\partial V}\right)_{\mathrm{T}}=T\left(\frac{\partial P}{\partial T}\right)_{\mathrm{V}}-P=T\left(\frac{\alpha_{\mathrm{p}}}{k_{\mathrm{T}}}\right)-P$
where $\alpha_{\mathrm{p}}$ is the isobaric expansivity and $k_{\mathrm{T}}$ is the isothermal compressibility of the mixture. For most of the liquids, the thermal pressure coefficient multiplied by absolute temperature, i.e., $T\left(\alpha_{\mathrm{p}} / k_{\mathrm{T}}\right)$ is very high so that the external pressure ( $P$ ) becomes negligible in comparison ${ }^{25,28,29}$, therefore it may be neglected in the Eq.(1) in the present calculations. Thus, the internal pressure can be shown to be equal to the following relationship ${ }^{28,29}$.
$\pi_{i}=\frac{\alpha_{\mathrm{p}} T}{k_{\mathrm{T}}}$

The free volume, $V_{\mathrm{f}}$ of the mixtures are calculated from the relation ${ }^{21,22,28,29}$
$V_{\mathrm{f}}=\frac{R T}{\left(P+\pi_{i}\right)}$
since $P$ is very small as compared to $\pi_{i}$, it has been neglected in the Eq.(3) in the present calculations. $k_{\mathrm{T}}$, is calculated using the well-known thermodynamic relationship ${ }^{31,32}$,
$k_{\mathrm{T}}=k_{\mathrm{s}}+\frac{T V \alpha_{\mathrm{p}}^{2}}{C_{\mathrm{p}}}$
where $k_{\mathrm{s}}\left[=1 /\left(u^{2} \rho\right)\right]$ is isentropic compressibility, $V$ is the molar volume and $C_{\mathrm{p}}$ is the heat capacity of the mixture. The $\alpha_{p}$ values for the mixtures were evaluated from temperature dependence of density data ${ }^{26}$. The $C_{\mathrm{p}}$ values of pure liquids have been taken from the literature ${ }^{33-35}$ and the $C_{\mathrm{p}}$ values for the mixtures have been calculated by using the following relationship.

$$
\begin{equation*}
C_{\mathrm{p}}=x_{1} C_{\mathrm{p}, 1}+x_{2} C_{\mathrm{p}, 2} \tag{5}
\end{equation*}
$$

The values of various parameters, $C_{\mathrm{p}}, \alpha_{\mathrm{p}}, k_{\mathrm{s}}$ and $k_{\mathrm{T}}$ of pure liquids used in the calculations are listed in Table S1 (Supplementary Data). The $\pi_{i}^{\mathrm{E}}$ and $V_{\mathrm{f}}^{\mathrm{E}}$ of binary mixtures have been calculated using the relationship,

$$
\begin{equation*}
Y^{E}=Y-\left(x_{1} Y_{1}+x_{2} Y_{2}\right) \tag{6}
\end{equation*}
$$

where Y is $\pi_{i}$ or $V_{\mathrm{f}}$ and subscripts 1 and 2 refers to pure $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]$ and alkanediol, respectively. The excess enthalpies ( $H^{\mathrm{E}}$ ) and excess entropies ( $S^{\mathrm{E}}$ ) are
calculated from $\pi_{i}$ and $V_{\mathrm{f}}$ by using the following relations based on regular solution theory ${ }^{21,22,35}$.
$-H^{\mathrm{E}}=\pi_{i} V-\left[x_{1} \pi_{i, 1} V_{1}+x_{2} \pi_{i, 2} V_{2}\right]$
$S^{\mathrm{E}}=R\left[x_{1} \ln V_{\mathrm{f}, 1}+x_{2} \ln V_{\mathrm{f}, 2}-\ln V_{\mathrm{f}}\right]$
The excess free energy ( $G^{\mathrm{E}}$ ) of mixtures is given by the relationship,
$G^{\mathrm{E}}=H^{\mathrm{E}}-T S^{\mathrm{E}}$
The values of $u, \rho, \pi_{i}$ and $V_{\mathrm{f}}$ for the binary mixtures of $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]+1,2$-propanediol/1,3-propanediol as functions of mole fraction, $x_{1}$ of $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]$ at various temperatures are listed in Table 1.

The experimental refractive indices ( $n_{\mathrm{D}}$ ) of [Bmim] $\left[\mathrm{BF}_{4}\right]+1,2$-propanediol/1,3-propanediol binary mixtures at investigated temperatures are included in Table 1. The deviations in refractive index, $\left(\Delta_{\phi} n_{\mathrm{D}}\right)$ and deviations in molar refractions ( $\Delta R_{\mathrm{M}}$ ) are calculated using the following relationship,

$$
\begin{equation*}
\Delta_{\phi} n_{\mathrm{D}}=n_{\mathrm{D}}-n_{\mathrm{D}}^{\mathrm{id}} \tag{10}
\end{equation*}
$$

where
$n_{\mathrm{D}}^{\text {id }}=\phi_{1} n_{\mathrm{D}, 1}+\phi_{2} n_{\mathrm{D}, 2}$

[^0]| [Bmim][BF $\left.{ }_{4}\right]+1,2$-propanediol |  |  |  |  |  | [Bmim][ BF $\left._{4}\right]+1,3$-propanediol |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $x_{1}$ | $\underset{\left(\mathrm{kg} \mathrm{~m}^{-3}\right)}{\rho}$ | $\begin{gathered} u \\ \left(\mathrm{~m} \mathrm{~s}^{-1}\right) \end{gathered}$ | $n_{\text {D }}$ | $\begin{gathered} \pi_{\mathrm{i}} \\ \left(10^{8} \mathrm{Nm}^{-2}\right) \end{gathered}$ | $\begin{gathered} V_{\mathrm{f}} \\ \left(10^{-6} \mathrm{~m}^{3} \mathrm{~mol}^{-1}\right) \end{gathered}$ | $x_{1}$ | $\underset{\left(\mathrm{kg} \mathrm{~m}^{-3}\right)}{\rho}$ | $\begin{gathered} u \\ \left(\mathrm{~m} \mathrm{~s}^{-1}\right) \end{gathered}$ | $n_{\mathrm{D}}$ | $\begin{gathered} \pi_{\mathrm{i}} \\ \left.10^{8} \mathrm{~N} \mathrm{~m}^{-2}\right) \end{gathered}$ | $\begin{gathered} V_{\mathrm{f}} \\ \left(10^{-6} \mathrm{~m}^{3} \mathrm{~mol}^{-1}\right) \end{gathered}$ |
| 298.15 K |  |  |  |  |  |  |  |  |  |  |  |
| 0.0000 | 1032.64 | 1510.97 | 1.43123 | 4.482 | 5.531 | 0.0000 | 1049.69 | 1628.79 | 1.43774 | 4.454 | 5.566 |
| 0.1034 | 1064.92 | 1518.52 | 1.42844 | 4.550 | 5.449 | 0.1021 | 1079.28 | 1612.75 | 1.43332 | 4.463 | 5.555 |
| 0.2030 | 1089.63 | 1524.65 | 1.42632 | 4.586 | 5.405 | 0.1994 | 1101.45 | 1601.09 | 1.43010 | 4.467 | 5.549 |
| 0.3050 | 1111.80 | 1530.55 | 1.42468 | 4.612 | 5.375 | 0.2991 | 1119.45 | 1589.97 | 1.42760 | 4.459 | 5.559 |
| 0.3835 | 1127.72 | 1535.09 | 1.42375 | 4.629 | 5.355 | 0.3989 | 1137.28 | 1580.80 | 1.42584 | 4.462 | 5.555 |
| 0.4936 | 1147.05 | 1541.08 | 1.42294 | 4.639 | 5.343 | 0.4970 | 1151.38 | 1574.21 | 1.42475 | 4.465 | 5.552 |
| 0.5811 | 1160.41 | 1545.77 | 1.42268 | 4.640 | 5.342 | 0.6057 | 1163.63 | 1569.19 | 1.42406 | 4.468 | 5.548 |
| 0.6878 | 1172.96 | 1550.74 | 1.42248 | 4.622 | 5.363 | 0.6828 | 1176.10 | 1565.19 | 1.42366 | 4.484 | 5.528 |
| 0.7997 | 1183.83 | 1555.93 | 1.42200 | 4.595 | 5.395 | 0.7928 | 1185.80 | 1563.54 | 1.42293 | 4.496 | 5.513 |
| 0.8818 | 1190.44 | 1559.96 | 1.42146 | 4.570 | 5.424 | 0.8974 | 1192.75 | 1564.24 | 1.42184 | 4.512 | 5.494 |
| 1.0000 | 1198.79 | 1564.92 | 1.42059 | 4.525 | 5.478 | 1.0000 | 1198.79 | 1565.09 | 1.42059 | 4.526 | 5.477 |
| 303.15 K |  |  |  |  |  |  |  |  |  |  |  |
| 0.0000 | 1028.95 | 1497.17 | 1.42951 | 4.478 | 5.629 | 0.0000 | 1046.55 | 1617.58 | 1.43631 | 4.468 | 5.641 |
| 0.1034 | 1061.15 | 1505.26 | 1.42674 | 4.548 | 5.542 | 0.1021 | 1075.88 | 1601.13 | 1.43184 | 4.473 | 5.635 |
| 0.2030 | 1085.54 | 1511.79 | 1.42464 | 4.586 | 5.496 | 0.1994 | 1097.92 | 1589.41 | 1.42859 | - 4.476 | 5.631 |
| 0.3050 | 1107.80 | 1518.02 | 1.42303 | 4.614 | 5.463 | 0.2991 | 1115.83 | 1578.24 | 1.42607 | - 4.467 | 5.642 |
| 0.3835 | 1123.53 | 1522.78 | 1.42213 | 4.631 | 5.443 | 0.3989 | 1133.59 | 1569.03 | 1.42430 | - 4.469 | $5.640$ <br> (Contd.) |

Table 1-The values of $\rho, u, n_{\mathrm{D}}, \pi_{i}$ and $V_{\mathrm{f}}$, for the binary mixtures of $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]+1,2$-propanediol/1,3-propaqnediol as a function of mole
fraction, $x_{1}$, of $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]$ at temperatures $\mathrm{T}=(298.15-318.15) \mathrm{K}$-Contd.

| [Bmim][BF $\left.{ }_{4}\right]+1,2$-propanediol |  |  |  |  |  | [Bmim][BF $\left.{ }_{4}\right]+1,3$-propanediol |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $x_{1}$ | $\stackrel{\rho}{\left(\mathrm{kg} \mathrm{~m}^{-3}\right)}$ | $\begin{gathered} u \\ \left(\mathrm{~m} \mathrm{~s}^{-1}\right) \end{gathered}$ | $n_{\text {D }}$ | $\begin{array}{cc} \pi_{\mathrm{i}} & V_{\mathrm{f}} \\ \left(10^{8} \mathrm{~N} \mathrm{~m}^{-2}\right) & \left(10^{-6} \mathrm{~m}^{3} \mathrm{~mol}^{-1}\right) \end{array}$ |  | $x_{1}$ | $\stackrel{\rho}{\left(\mathrm{kg} \mathrm{~m}^{-3}\right)}$ | $\begin{gathered} u \\ \left(\mathrm{~m} \mathrm{~s}^{-1}\right) \end{gathered}$ | $\begin{array}{cc} \hline \pi_{\mathrm{i}} & V_{\mathrm{f}} \\ \left(10^{8} \mathrm{~N} \mathrm{~m}^{-2}\right) & \left(10^{-6} \mathrm{~m}^{3} \mathrm{~mol}^{-1}\right) \end{array}$ |  |  |
| 303.15 K |  |  |  |  |  |  |  |  |  |  |  |
| 0.4936 | 1142.88 | 1529.00 | 1.42133 | 4.643 | 5.429 | 0.4970 | 1147.66 | 1562.41 | 1.42319 | 4.471 | 5.637 |
| 0.5811 | 1156.26 | 1533.82 | 1.42108 | 4.644 | 5.427 | 0.6057 | 1159.89 | 1557.38 | 1.42251 | 4.474 | 5.633 |
| 0.6878 | 1169.03 | 1538.89 | 1.42092 | 4.628 | 5.446 | 0.6828 | 1172.38 | 1553.39 | 1.42212 | 4.490 | 5.614 |
| 0.7997 | 1180.06 | 1544.10 | 1.42048 | 4.601 | 5.478 | 0.7928 | 1182.13 | 1551.77 | 1.42140 | 4.502 | 5.598 |
| 0.8818 | 1186.82 | 1548.10 | 1.41996 | 4.576 | 5.508 | 0.8974 | 1189.17 | 1552.52 | 1.42033 | 4.519 | 5.578 |
| 1.0000 | 1195.19 | 1552.93 | 1.41914 | 4.530 | 5.563 | 1.0000 | 1195.19 | 1553.15 | 1.41914 | 4.531 | 5.562 |
| 308.15 K |  |  |  |  |  |  |  |  |  |  |  |
| 0.0000 | 1025.20 | 1483.12 | 1.42762 | 4.471 | 5.731 | 0.0000 | 1043.41 | 1606.18 | 1.43489 | 4.480 | 5.719 |
| 0.1034 | 1057.16 | 1491.81 | 1.42490 | 4.543 | 5.639 | 0.1021 | 1072.51 | 1589.64 | 1.43034 | 4.483 | 5.715 |
| 0.2030 | 1081.55 | 1498.77 | 1.42285 | 4.583 | 5.590 | 0.1994 | 1094.44 | 1577.80 | 1.42706 | 4.484 | 5.713 |
| 0.3050 | 1103.82 | 1505.35 | 1.42130 | 4.613 | 5.554 | 0.2991 | 1112.27 | 1566.52 | 1.42452 | 4.474 | 5.727 |
| 0.3835 | 1119.46 | 1510.36 | 1.42043 | 4.631 | 5.532 | 0.3989 | 1129.96 | 1557.23 | 1.42276 | 4.475 | 5.726 |
| 0.4936 | 1138.72 | 1516.86 | 1.41965 | 4.644 | 5.517 | 0.4970 | 1143.99 | 1550.57 | 1.42162 | 4.476 | 5.723 |
| 0.5811 | 1152.12 | 1521.85 | 1.41942 | 4.646 | 5.514 | 0.6057 | 1156.21 | 1545.51 | 1.42093 | 4.479 | 5.720 |
| 0.6878 | 1165.24 | 1527.05 | 1.41930 | 4.632 | 5.531 | 0.6828 | 1168.70 | 1541.52 | 1.42055 | 4.494 | 5.701 |
| 0.7997 | 1176.31 | 1532.34 | 1.41891 | 4.605 | 5.563 | 0.7928 | 1178.49 | 1539.93 | 1.41984 | 4.507 | 5.685 |
| 0.8818 | 1183.22 | 1536.34 | 1.41842 | 4.581 | 5.592 | 0.8974 | 1185.59 | 1540.75 | 1.41881 | 4.523 | 5.664 |
| 1.0000 | 1191.61 | 1541.18 | 1.41765 | 4.535 | 5.649 | 1.0000 | 1191.61 | 1541.35 | 1.41765 | 4.536 | 5.648 |
| 313.15 K |  |  |  |  |  |  |  |  |  |  |  |
| 0.0000 | 1021.43 | 1469.03 | 1.42594 | 4.461 | 5.836 | 0.0000 | 1040.24 | 1594.83 | 1.43337 | 4.491 | 5.798 |
| 0.1034 | 1053.35 | 1478.35 | 1.42322 | 4.537 | 5.738 | 0.1021 | 1069.14 | 1578.11 | 1.42877 | 4.491 | 5.797 |
| 0.2030 | 1077.48 | 1485.70 | 1.42120 | 4.578 | 5.687 | 0.1994 | 1090.96 | 1566.18 | 1.42547 | 4.491 | 5.797 |
| 0.3050 | 1099.83 | 1492.64 | 1.41968 | 4.610 | 5.647 | 0.2991 | 1108.71 | 1554.83 | 1.42294 | 4.479 | 5.813 |
| 0.3835 | 1115.37 | 1497.88 | 1.41883 | 4.629 | 5.624 | 0.3989 | 1126.35 | 1545.49 | 1.42118 | 4.479 | 5.813 |
| 0.4936 | 1134.49 | 1504.66 | 1.41808 | 4.643 | 5.607 | 0.4970 | 1140.34 | 1538.80 | 1.42006 | 4.480 | 5.811 |
| 0.5811 | 1147.90 | 1509.83 | 1.41785 | 4.646 | 5.603 | 0.6057 | 1152.54 | 1533.74 | 1.41936 | 4.482 | 5.809 |
| 0.6878 | 1161.36 | 1515.18 | 1.41776 | 4.634 | 5.618 | 0.6828 | 1165.04 | 1529.76 | 1.41901 | 4.497 | 5.789 |
| 0.7997 | 1172.68 | 1520.58 | 1.41741 | 4.609 | 5.649 | 0.7928 | 1174.87 | 1528.21 | 1.41833 | 4.510 | 5.773 |
| 0.8818 | 1179.64 | 1524.63 | 1.41694 | 4.585 | 5.679 | 0.8974 | 1182.04 | 1529.09 | 1.41732 | 4.527 | 5.751 |
| 1.0000 | 1188.05 | 1529.52 | 1.41622 | 4.539 | 5.736 | 1.0000 | 1188.05 | 1529.69 | 1.41622 | 4.540 | 5.735 |
| 318.15 K |  |  |  |  |  |  |  |  |  |  |  |
| 0.0000 | 1017.63 | 1454.91 | 1.42420 | 4.445 | 5.951 | 0.0000 | 1037.06 | 1583.48 | 1.43190 | 4.500 | 5.878 |
| 0.1034 | 1049.42 | 1464.89 | 1.42148 | 4.525 | 5.846 | 0.1021 | 1065.77 | 1566.64 | 1.42723 | 4.498 | 5.880 |
| 0.2030 | 1073.43 | 1472.67 | 1.41950 | 4.568 | 5.790 | 0.1994 | 1087.49 | 1554.63 | 1.42389 | 4.497 | 5.882 |
| 0.3050 | 1095.70 | 1479.97 | 1.41800 | 4.603 | 5.747 | 0.2991 | 1105.17 | 1543.21 | 1.42135 | 4.484 | 5.899 |
| 0.3835 | 1111.20 | 1485.48 | 1.41717 | 4.623 | 5.721 | 0.3989 | 1122.75 | 1533.83 | 1.41960 | 4.483 | 5.901 |
| 0.4936 | 1130.34 | 1492.55 | 1.41644 | 4.639 | 5.701 | 0.4970 | 1136.71 | 1527.12 | 1.41845 | 4.483 | 5.900 |
| 0.5811 | 1143.50 | 1497.92 | 1.41620 | 4.643 | 5.697 | 0.6057 | 1148.90 | 1522.06 | 1.41776 | 4.485 | 5.898 |
| 0.6878 | 1157.40 | 1503.43 | 1.41616 | 4.634 | 5.709 | 0.6828 | 1161.40 | 1518.11 | 1.41741 | 4.500 | 5.878 |
| 0.7997 | 1168.97 | 1508.95 | 1.41585 | 4.610 | 5.738 | 0.7928 | 1171.27 | 1516.62 | 1.41678 | 4.513 | 5.861 |
| 0.8818 | 1176.07 | 1513.05 | 1.41541 | 4.587 | 5.766 | 0.8974 | 1178.50 | 1517.59 | 1.41578 | 4.531 | 5.838 |
| 1.0000 | 1184.51 | 1518.02 | 1.41473 | 4.542 | 5.823 | 1.0000 | 1184.51 | 1518.19 | 1.41473 | 4.543 | 5.822 |
| 323.15 K |  |  |  |  |  |  |  |  |  |  |  |
| 0.0000 | 1013.79 | 1440.73 | 1.42248 | 4.427 | 6.069 | 0.0000 | 1033.87 | 1572.11 | 1.43044 | 4.508 | 5.960 |
| 0.1034 | 1044.98 | 1451.40 | 1.41978 | 4.509 | 5.958 | 0.1021 | 1062.39 | 1555.15 | 1.42570 | 4.504 | 5.965 |
| 0.2030 | 1069.42 | 1459.63 | 1.41783 | 4.557 | 5.895 | 0.1994 | 1084.01 | 1543.09 | 1.42234 | 4.501 | 5.969 |
| 0.3050 | 1091.56 | 1467.33 | 1.41637 | 4.594 | 5.848 | 0.2991 | 1101.63 | 1531.63 | 1.41980 | 4.487 | 5.988 |
| 0.3835 | 1107.05 | 1473.11 | 1.41556 | 4.617 | 5.820 | 0.3989 | 1119.16 | 1522.22 | 1.41805 | 4.485 | 5.990 |
| 0.4936 | 1126.22 | 1480.50 | 1.41485 | 4.635 | 5.797 | 0.4970 | 1133.09 | 1515.51 | 1.41690 | 4.485 | 5.990 |
| 0.5811 | 1139.42 | 1486.07 | 1.41462 | 4.640 | 5.790 | 0.6057 | 1145.27 | 1510.46 | 1.41620 | 4.486 | 5.989 |
| 0.6878 | 1153.56 | 1491.76 | 1.41461 | 4.633 | 5.799 | 0.6828 | 1157.79 | 1506.55 | 1.41588 | 4.501 | 5.969 |
| 0.7997 | 1165.28 | 1497.42 | 1.41435 | 4.611 | 5.827 | 0.7928 | 1167.69 | 1505.13 | 1.41528 | 4.515 | 5.951 |
| 0.8818 | 1172.53 | 1501.56 | 1.41395 | 4.589 | 5.854 | 0.8974 | 1174.98 | 1506.18 | 1.41431 | 4.533 | 5.927 |
| 1.0000 | 1180.98 | 1506.62 | 1.41331 | 4.544 | 5.912 | 1.0000 | 1180.98 | 1506.80 | 1.41331 | 4.545 | 5.911 |

Here $\phi$ is the volume fraction and $V_{\mathrm{m}}$ is the molar volume of the mixture and are calculated using the relationship.

$$
\begin{equation*}
\phi_{i}=x_{i} V_{\mathrm{m}, i} / \sum_{i=1}^{2} x_{i} V_{\mathrm{m}, i} \tag{12}
\end{equation*}
$$

The values of $\phi_{i}, \pi_{i}^{\mathrm{E}}, V_{\mathrm{f}}^{\mathrm{E}}, H^{\mathrm{E}}, T S^{\mathrm{E}}, G^{\mathrm{E}}$ and $\Delta_{\phi} n_{\mathrm{D}}$ for the mixtures are listed in Tables S2 and S3 (Supplementary Data). The values of $\pi_{i}^{\mathrm{E}}, V_{\mathrm{f}}^{\mathrm{E}}, H^{\mathrm{E}}$, $T S^{\mathrm{E}}, G^{\mathrm{E}}$ and $\Delta_{\phi} n_{\mathrm{D}}$ were fitted to a Redlich-Kister ${ }^{36}$ type polynomial equation

$$
\begin{equation*}
Y^{\mathrm{E}}=x_{1}\left(1-x_{1}\right) \sum_{i=1}^{n} A_{i}\left(2 x_{1}-1\right)^{i-1} \tag{13}
\end{equation*}
$$

where $Y^{\mathrm{E}}$ is $\pi_{i}^{\mathrm{E}}$ or $V_{\mathrm{f}}^{\mathrm{E}}$ or $H^{\mathrm{E}}$ or $T S^{\mathrm{E}}$ or $G^{\mathrm{E}}$ or $\Delta_{\phi} n_{\mathrm{D}}$. The volume fraction, $\phi$, was used instead of $x$ for fitting of $\Delta_{\phi} n_{\mathrm{D}}$. The values of coefficients, $A_{i}$ in Eq. (13) were evaluated by using least-squares method with all points weighted equally. The values of coefficients, $A_{i}$ of Eq.(13) for the excess functions and the corresponding standard deviations, $\sigma$ are listed in Table 2. The variation of $\pi_{i}^{\mathrm{E}}, V_{\mathrm{f}}^{\mathrm{E}}, H^{\mathrm{E}}$, $T S^{\mathrm{E}}, G^{\mathrm{E}}$ and $\Delta_{\phi} n_{\mathrm{D}}$ with composition and temperature of the mixtures are presented graphically in Figs 1-6, respectively.

## Mixing rules for predicting refractive index

The refractive indices of the binary mixtures have been theoretically calculated from the refractive index data of pure components of the mixtures using various mixing rules ${ }^{37-39}$.

Table 2-Coefficients ( $A_{i}$ ) of Eq. (13) for $\pi_{i}^{\mathrm{E}}, V_{\mathrm{f}}^{\mathrm{E}}, H^{\mathrm{E}}, T S^{\mathrm{E}}, G^{\mathrm{E}}$ and $\Delta_{\phi}{ }^{n}$ D along with standard deviations ( $\sigma$ ) for [Bmim $]\left[\mathrm{BF}_{4}\right]+1,2$-propandiol/1,3-propanediol binary mixtures at different temperatures


Table 2-Coefficients ( $A_{i}$ ) of Eq. (13) for $\pi_{i}^{\mathrm{E}}, V_{\mathrm{f}}^{\mathrm{E}}, H^{\mathrm{E}}, T S^{\mathrm{E}}, G^{\mathrm{E}}$ and $\Delta_{\phi}{ }^{n} \mathrm{D}$ along with standard deviations ( $\sigma$ ) for
$[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]+1,2$-propandiol/1,3-propanediol binary mixtures at different temperatures-Contd.

| Property | $T$ (K) | $A_{1}$ | $A_{2}$ | $A_{3}$ | $A_{4}$ | $A_{5}$ | $\sigma$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\Delta_{\phi} n_{D}\left(10^{-2}\right)$ | 298.15 | -0.4580 | -0.2732 | 0.7142 | 1.2375 | - | 0.0054 |
|  | 303.15 | -0.4849 | -0.2866 | 0.6903 | 1.2234 | - | 0.0057 |
|  | 308.15 | -0.5046 | -0.3011 | 0.6513 | 1.2238 | - | 0.0059 |
|  | 313.15 | -0.5317 | -0.3044 | 0.6177 | 1.2054 | - | 0.0059 |
|  | 318.15 | -0.5573 | -0.3291 | 0.5696 | 1.2400 | - | 0.0060 |
|  | 323.15 | -0.5841 | -0.3467 | 0.5339 | 1.2417 | - | 0.0060 |
| $[B m i m]\left[B F_{4}\right]+1,2-P$ |  |  |  |  |  |  |  |
| $\pi_{i}^{\mathrm{E}}\left(10^{8} \mathrm{~N} \mathrm{~m}^{-2}\right)$ | 298.15 | -0.1042 | -0.0377 | 0.1343 | -0.0397 | - | 0.0024 |
|  | 303.15 | -0.1181 | -0.0326 | 0.1343 | -0.0151 | - | 0.0025 |
|  | 308.15 | -0.1320 | -0.0312 | 0.1394 | -0.0091 | - | 0.0025 |
|  | 313.15 | -0.1457 | -0.0298 | 0.1403 | 0.0006 | - | 0.0025 |
|  | 318.15 | -0.1591 | -0.0285 | 0.1430 | 0.0098 | - | 0.0025 |
|  | 323.15 | -0.1719 | -0.0270 | 0.1449 | 0.0181 | - | 0.0025 |
| $V_{\mathrm{f}}^{\mathrm{E}}\left(10^{-6} \mathrm{~m}^{3} \mathrm{~mol}^{-1}\right)$ | 298.15 | 0.1276 | 0.0449 | -0.1681 | 0.0500 | - | 0.0030 |
|  | 303.15 | 0.1468 | 0.0392 | -0.1698 | 0.0204 | - | 0.0031 |
|  | 308.15 | 0.1666 | 0.0381 | -0.1782 | 0.0119 | - | 0.0032 |
|  | 313.15 | 0.1869 | 0.0367 | -0.1821 | -0.0013 | - | 0.0032 |
|  | 318.15 | 0.2072 | 0.0353 | -0.1889 | -0.0116 | - | 0.0033 |
|  | 323.15 | 0.2272 | 0.0340 | -0.1944 | -0.0234 | - | 0.0034 |
| $H^{\mathrm{E}}\left(\mathrm{kJ} \mathrm{mol}^{-1}\right)$ | 298.15 | 1.2732 | 2.5313 | 0.6317 | -0.8625 | -1.7366 | 0.0310 |
|  | 303.15 | 1.3017 | 2.5407 | 0.6245 | -1.0942 | -1.8482 | 0.0321 |
|  | 308.15 | 1.3526 | 2.6025 | 0.6242 | -1.1598 | -1.9749 | 0.0327 |
|  | 313.15 | 1.4138 | 2.6545 | 0.6262 | -1.2420 | -2.0448 | 0.0333 |
|  | 318.15 | 1.4801 | 2.7113 | 0.6241 | -1.3187 | -2.1295 | 0.0338 |
|  | 323.15 | 1.5488 | 2.7635 | 0.6196 | -1.3985 | -2.2074 | 0.0343 |
| $T S^{\mathrm{E}}\left(10^{-2} \mathrm{~J} \mathrm{~mol}^{-1}\right)$ | 298.15 | 0.5741 | 0.2047 | -0.7469 | 0.2227 | - | 0.0136 |
|  | 303.15 | 0.6605 | 0.1787 | -0.7564 | 0.0898 | - | 0.0139 |
|  | 308.15 | 0.7502 | 0.1752 | -0.7971 | 0.0525 | - | 0.0141 |
|  | 313.15 | 0.8420 | 0.1682 | -0.8169 | -0.0049 | - | 0.0144 |
|  | 318.15 | 0.9337 | 0.1621 | -0.8452 | -0.0520 | - | 0.0147 |
|  | 323.15 | 1.0249 | 0.1564 | -0.8711 | -0.1065 | - | 0.0150 |
| $G^{\mathrm{E}}\left(\mathrm{kJ} \mathrm{mol}^{-1}\right)$ | 298.15 | 0.7501 | 2.3271 | 0.4493 | -1.0899 | - | 0.0394 |
|  | 303.15 | 0.6956 | 2.3618 | 0.3921 | -1.1872 | - | 0.0403 |
|  | 308.15 | 0.6604 | 2.4271 | 0.3658 | -1.2159 | - | 0.0411 |
|  | 313.15 | 0.5647 | 2.4862 | 1.5739 | -1.2367 | -2.2887 | 0.0416 |
|  | 318.15 | 0.5398 | 2.5483 | 1.5879 | -1.2641 | -2.3512 | 0.0421 |
|  | 323.15 | 0.5176 | 2.6078 | 1.6058 | -1.2929 | -2.4225 | 0.0425 |
| $\Delta_{\phi} n_{D}\left(10^{-2}\right)$ | 298.15 | -0.5895 | -0.2533 | 0.9709 | 1.6578 | - | 0.0043 |
|  | 303.15 | -0.6250 | -0.2718 | 0.9409 | 1.6127 | - | 0.0047 |
|  | 308.15 | -0.6598 | -0.2769 | 0.8992 | 1.5771 | - | 0.0046 |
|  | 313.15 | -0.7033 | -0.2814 | 0.8710 | 1.5274 | - | 0.0050 |
|  | 318.15 | -0.7464 | -0.2941 | 0.8386 | 1.4952 | - | 0.0057 |
|  | 323.15 | -0.7909 | -0.3066 | 0.7952 | 1.4734 | - | 0.0061 |

Arago-Biot (A-B)

$$
\begin{equation*}
n=n_{1} \phi_{1}+n_{2} \phi_{2} \tag{14}
\end{equation*}
$$

Gladstone-Dale (G-D)
$n-1=\left(n_{1}-1\right) \varphi_{1}+\left(n_{2}-1\right) \varphi_{2}$

Newton's (N) relationship
$n^{2}-1=\left(n_{1}^{2}-1\right) \phi_{1}+\left(n_{2}^{2}-1\right) \phi_{2}$
Eyring and John (E-J)
$n=n_{1} \phi_{1}^{2}+2\left(n_{1} n_{2}\right)^{1 / 2} \phi_{1} \phi_{2}+n_{2} \phi_{2}^{2}$

Table 3-Average percentage deviations (APD) in Arago-Biot (A-B), Gladstone-Dale (G-D), Newton (N), Eyring-John (E-J),
Lorentz-Lorentz (L-L), Heller (H), Eykman (EK), Oster (OS) and Weiner (W) relationships for [Bmim] $\left.\mathrm{BF}_{4}\right]+1,2$-propandiol/ 1,3-propanediol binary mixtures at different temperatures

| $T$ (K) | A-B | G-D | N | E-J | L-L | H | EK | OS | W |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\left[{\text { Bmin }]\left[B F_{4}\right.}_{4}\right]+1,2$-propanediol |  |  |  |  |  |  |  |  |  |
| 298.15 | 0.0427 | 0.0427 | 0.0430 | 0.0425 | 0.0423 | 0.0424 | 0.0419 | 0.0417 | 0.0426 |
| 303.15 | 0.0448 | 0.0448 | 0.0451 | 0.0446 | 0.0445 | 0.0445 | 0.0441 | 0.0439 | 0.0447 |
| 308.15 | 0.0464 | 0.0464 | 0.0467 | 0.0463 | 0.0461 | 0.0462 | 0.0458 | 0.0456 | 0.0463 |
| 313.15 | 0.0488 | 0.0488 | 0.0491 | 0.0486 | 0.0484 | 0.0485 | 0.0480 | 0.0478 | 0.0486 |
| 318.15 | 0.0522 | 0.0522 | 0.0525 | 0.0521 | 0.0519 | 0.0520 | 0.0515 | 0.0513 | 0.0521 |
| 323.15 | 0.0557 | 0.0557 | 0.0560 | 0.0555 | 0.0554 | 0.0555 | 0.0550 | 0.0548 | 0.0556 |
| [Bmin $]\left[B F_{4}\right]+1,3$-propanediol |  |  |  |  |  |  |  |  |  |
| 298.15 | 0.0555 | 0.0555 | 0.0563 | 0.0551 | 0.0546 | 0.0548 | 0.0536 | 0.0531 | 0.0552 |
| 303.15 | 0.0578 | 0.0578 | 0.0586 | 0.0574 | 0.0570 | 0.0571 | 0.0559 | 0.0554 | 0.0575 |
| 308.15 | 0.0604 | 0.0604 | 0.0612 | 0.0600 | 0.0595 | 0.0597 | 0.0585 | 0.0579 | 0.0601 |
| 313.15 | 0.0635 | 0.0635 | 0.0643 | 0.0631 | 0.0627 | 0.0628 | 0.0616 | 0.0611 | 0.0632 |
| 318.15 | 0.0679 | 0.0679 | 0.0689 | 0.0674 | 0.0668 | 0.0671 | 0.0655 | 0.0648 | 0.0675 |
| 323.15 | 0.0730 | 0.0730 | 0.0740 | 0.0724 | 0.0719 | 0.0722 | 0.0706 | 0.0699 | 0.0726 |

Lorentz-Lorentz (L-L)
$\frac{n^{2}-1}{n^{2}+2}=\left(\frac{n_{1}^{2}-1}{n_{1}^{2}+2}\right) \phi_{1}+\left(\frac{n_{2}^{2}-1}{n_{2}^{2}+2}\right) \phi_{2}$
Heller (H):
$\frac{n-n_{1}}{n_{1}}=\frac{3}{2}\left[\frac{\left(n_{2} / n_{1}\right)^{2}-1}{\left(n_{2} / n_{1}\right)^{2}+2}\right] \phi_{2}$
Eykman (EK)

$$
\begin{equation*}
\frac{n^{2}-1}{n+0.4}=\left(\frac{n_{1}^{2}-1}{n_{1}+0.4}\right) \phi_{1}+\left(\frac{n_{2}^{2}-1}{n_{2}+0.4}\right) \phi_{2} \tag{20}
\end{equation*}
$$

Oster (OS):
$\frac{\left(n^{2}-1\right)\left(2 n^{2}+1\right)}{n^{2}}=\frac{\left(n_{1}^{2}-1\right)\left(2 n_{1}^{2}+1\right)}{n_{1}^{2}} \phi_{1}$
$+\frac{\left(n_{2}^{2}-1\right)\left(2 n_{2}^{2}+1\right)}{n_{2}^{2}} \phi_{2}$
Weiner (W)

$$
\begin{equation*}
\frac{n^{2}-n_{1}^{2}}{n^{2}+2 n_{2}^{2}}=\left(\frac{n^{2}-n_{1}^{2}}{n_{2}^{2}+2 n_{1}^{2}}\right) \phi_{2} \tag{22}
\end{equation*}
$$

where $n$ represents the refractive index $\left(n_{\mathrm{D}}\right)$ in the relations (14)-(22) The refractive indices obtained from Eqs.(17)-(22) have been compared with the experimental values and the results are presented in terms of average percentage deviations (APD) calculated using the relationship,

$$
\begin{equation*}
A P D=\frac{1}{m}\left[\sum \frac{\left(n_{\text {Expt }}-n_{\text {Calc }}\right)}{n_{\text {Expt. }}} \times 100\right] \tag{23}
\end{equation*}
$$

where m is number of data points. The APDs for the binary systems at investigated temperatures are listed in Table 3.

## Excess internal pressure

The results shown in Fig. 1 indicate that the $\pi_{i}^{\mathrm{E}}$ values are positive for $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]+1,2$-propanediol and negative for $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]+1,3$-propanediol over entire mole fraction range and at all investigated temperatures. As stated earlier, the molecules of alkanediols are associated through inter- and intramolecular hydrogen bonding in pure state ${ }^{40}$. Mixing of $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]$ with alkanediols would induce mutual dissociation of the hydrogen-bonded structures present in pure alkanediols with subsequent formation of hydrogen bonding and ion-dipole interactions between unlike molecules. The observed positive $\pi_{i}^{\mathrm{E}}$ values for $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]+1,2$-propanediol (Fig. 1) can be considered due to the formation of hydrogen bonding between $\left[\mathrm{Bmim}^{+} /\left[\mathrm{BF}_{4}\right]^{-}\right.$ions and 1,2-propanediol molecules that leads to closer packing of molecules, resulting in a contraction in volume of the mixture, leading to an increase in the internal pressure of the mixture, hence, positive $\pi_{i}^{\mathrm{E}}$ values. The negative $\pi_{i}^{\mathrm{E}}$ values for $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]+1,3$-propanediol mixtures indicate weaker interactions between $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]$ and 1,3 -propanediol molecules. The magnitude of $\pi_{i}^{\mathrm{E}}$ values for $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]+$


Fig. 1-Variation of excess internal pressure, $\pi_{i}^{\mathrm{E}}$ with mole fraction, $x_{1}$ of $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]$ for the (a) $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]+$ 1,2-propandiol and (b) $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]+1,3$-propanediol binary mixtures at different temperatures.

1,2-propanediol and 1,3-propanediol mixtures follows the sequence: 1,2-propanediol > 1,3-propanediol, which indicates the order of interactions in these systems.

## Excess free volume

The perusal of Fig. 2 indicates that the $V_{\mathrm{f}}^{\mathrm{E}}$ values are positive for $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]+1,3$-propanediol and negative for $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]+1$,2-propanediol mixtures over the entire composition range and at all temperatures. The observed trends in $V_{f}^{\mathrm{E}}$ value indicate specific interactions in $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]+$ 1,2-propanediol, and weak interactions in [Bmim $]\left[\mathrm{BF}_{4}\right]+1$,3-propanediol mixtures. But opposite to our expectation, the positive trends are observed in $V_{\mathrm{f}}^{\mathrm{E}}$ values for $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]+1,3$-propanediol (Fig. 2) over the entire composition range. The results can be explained in terms of molecular interactions, structural effects and interstitial accommodation along with the changes in free volume. The sign of the $V_{\mathrm{f}}^{\mathrm{E}}$ depends on the relative strength between the contractive and


Fig. 2-Variation of excess free volume, $V_{\mathrm{f}}^{\mathrm{E}}$ with mole fraction, $x_{1}$ of $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]$ for (a) $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]+1,2$-propandiol and (b) $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]+1,3$-propanediol binary mixtures at different temperatures.
expansive forces. The factors responsible for volume contraction are (i) specific interactions between the component molecules and (ii) weak physical forces, such as ion-dipole or dipole-dipole interactions or van der Waals forces. The factors that cause expansion in volume are dispersive forces, steric hindrance of component molecules, unfavorable geometric fitting and electrostatic repulsion. The negative values of excess free volume in binary system assert that the combined effects of the factors are responsible for volume contraction and vice-versa ${ }^{41}$. According to these investigations, the positive values of excess free volume (Fig. 2) may be arising from the formation of weaker IL-solvent than IL-IL and solvent-solvent interactions in the liquid mixtures and the negative (Fig. 2) values of excess free volume may be attributed to the packing effect and ion-dipole interaction of solvent molecules with the IL in these mixtures ${ }^{42,43}$.

## Excess enthalpy of mixing

In general, $H^{\mathrm{E}}$ values of mixing depend upon the relative enthalpies of endothermic and exothermic
effects that arise on mixing of the components. The factors that cause endothermic effect on mixing are:
a) strong specific interactions, usually some type of chemical interactions,
b) favourable geometrical fitting of component molecules due to occupation of void spaces of one component by the other when the molecular sizes of the unlike molecules differ by a large magnitude, and,
c) ion-dipole interactions of solvent molecules with the ionic liquid molecules.
The factors that cause exothermic effect on mixing of the components are:
a) breakdown of the solvent self-associated molecules from each other,
b) breakdown of the ionic liquid ion pairs, and,
c) formation of weaker ionic liquid-solvent bonds than ionic liquid-ionic liquid and solvent-solvent bonds.
It can be observed that the negative value of $H^{\mathrm{E}}$ indicate exothermic process, and positive value of $H^{\mathrm{E}}$ indicates endothermic process in the mixing of the $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]$ with $\alpha, \omega$-propanediols systems. Figure 3 shows that the excess molar enthalpies are exothermic for $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]+1,2$-propanediol mixtures with the maxima being exhibited in the equimolar region; while it is endothermic for $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]+1,2$-propanediol mixtures over the entire composition and at each investigated temperature ${ }^{44}$. The positive $H^{\mathrm{E}}$ values may be attributed due to the packing effect and ion-dipole interaction of solvent molecules with the ionic liquid in liquid mixture ${ }^{45}$. The negative $H^{\mathrm{E}}$ values may be attributed to dipole-dipole or ion-ion interactions between the solvent molecules and ionic liquids and are dominant over the ion-dipole interaction between unlike molecules. Also, the dissociation of hydrogen bonding in the alkanediols molecules dominates over the formation of intermolecular bonding between the ionic liquid and alkanediols, and the dissociation of the ionic liquid ion pairs ${ }^{46}$. The magnitude of $H^{\mathrm{E}}$ follows the sequence: 1, 2-proanediol < 1, 3-proanediol.

## Excess entropy of mixing

The $T S^{\mathrm{E}}$ values for $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]+1,2$-propanediol are negative while the values for $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]+$ 1,3-propanediol are positive over the entire composition range at each investigated temperature (Fig. 4). The negative $T S^{\mathrm{E}}$ values for [Bmim][BF4]+1,2-propanediol


Fig. 3-Variation of excess enthalpy, $H^{\mathrm{E}}$ with mole fraction, $x_{1}$, of $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]$ for (a) $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]+1,2$-propandiol and (b) $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]+1,3$-propanediol binary mixtures at different temperatures.


Fig. 4-Variation of excess entropy, $T S^{\mathrm{E}}$ with mole fraction, $x_{1}$ of $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]$ for (a) $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]+1,2$-propandiol and (b) $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]+1,3$-propanediol binary mixtures at different temperatures.


Fig. 5-Variation of excess free energy, $G^{\mathrm{E}}$ with mole fraction, $x_{1}$ of $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]$ for (a) $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]+1,2$-propandiol and (b) $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]+1,3$-propanediol binary mixtures at different temperatures.
mixtures further support the conclusions drawn from the $\pi_{\mathrm{i}}^{\mathrm{E}}$ and $V_{\mathrm{f}}^{\mathrm{E}}$ values, that the formation of hydrogen bonding between $[\mathrm{Bmim}]^{+} /[\mathrm{BF} 4]^{-}$ions and 1,2-propanediol molecules leads to closer packing of molecules, resulting in a contraction in volume. This leads to a decrease in the entropy of the mixture resulting in negative $T S^{\mathrm{E}}$ values. The positive values of $T S^{\mathrm{E}}$ may be attributed to the disruption of hydrogen bonded associates of propanediols that dominate the hydrogen bonding between unlike molecules.

## Excess free energy of mixing

The $G^{\mathrm{E}}$ values for $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]+1,2$-propanediol are negative, while the values for $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]+$ 1,3-propanediol are positive over the entire composition range at each investigated temperature (Fig. 5). The positive values $G^{\mathrm{E}}$ suggest the existence of weak ion-dipole interactions between $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]$ and 1,3 -propanediol molecules while the negative values of $G^{\mathrm{E}}$ may be attributed to effective geometrical packing effect and formation of hydrogen bonding between $[\mathrm{Bmim}]^{+} /\left[\mathrm{BF}_{4}\right]^{-}$ions and 1,2-propanediol molecules in the mixtures.


Fig. 6-Variation of deviations in refractive index, $\Delta_{\phi}{ }^{n}$ with volume fraction, $\phi_{1}$ of $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]$ for (a) $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]+$ 1,2-propandiol and (b) $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]+1,3$-propanediol binary mixtures at different temperatures.

## Deviations in refractive index

The refractive index $n_{\mathrm{D}}$ can be used as a measure of the electronic polarizability of a molecule and can provide useful information when studying the interaction between molecules. In general, the positive deviations in $\Delta_{\phi} n_{\mathrm{D}}$ values are considered due to the presence of significant interactions in the mixtures,
whereas the negative deviations in $\Delta_{\phi} n_{\mathrm{D}}$ values indicate weak interactions between the components of the mixture ${ }^{47}$. A perusal of Fig. 6 shows that the $\Delta_{\phi} n_{\mathrm{D}}$ values are negative in the mole fraction region of $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]\left(x_{1}<0.8\right)$ and are positive at the higher mole fractions $\left(x_{1}>0.8\right)$ at all investigated temperatures. The mixing of $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]$ with alkanediols leads to mutual dissociation of the hydrogen-bonded structures present in pure alkanediols with subsequent formation of new hydrogen bonding and ion-dipole interactions between unlike molecules. The negative $\Delta_{\phi} n_{\mathrm{D}}$ values in the mole fraction region of $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]\left(x_{1}<0.8\right)$ may be attributed to the dominance of disruption of hydrogen bonded associates between propanediol molecules over iondipole interactions between $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]$ and propanediol molecules in the mixtures. The $\Delta_{\phi} n_{\mathrm{D}}$ values decrease with increase in temperature for each binary mixture, indicating that the interactions decrease due to breaking of hydrogen bonds in propanediol. Also, the $\Delta_{\phi} n_{\mathrm{D}}$ values are found opposite to the sign of excess molar volumes $V_{\mathrm{m}}^{\mathrm{E}}$ for all these binary mixtures ${ }^{26}$, which is in agreement with the view proposed by Brocos et al. ${ }^{48,49}$. This further reinforces the conclusions drawn regarding intermolecular interactions from the variations of $V_{m}^{\mathrm{E}}$ values in our earlier study ${ }^{26}$ on these mixtures.

A perusal of Table 3 indicates that the APDs between the experimental values of refractive indices of these mixtures and theoretically calculated values from various mixing rules are low in the range of 0.042 to 0.056 for $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]+1$,2-propanediol and 0.053 to 0.074 for $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]+1,3$-propanediol. The low values of APDs clearly indicate the applicability of various mixing rules for the binary mixtures under study.

## Conclusions

The refractive indices $\left(n_{\mathrm{D}}\right)$ of the binary mixtures of $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]$ with $\alpha, \omega$-propanediols have been measured over the entire composition range at temperatures from 298.15 to 323.15 K . Using the experimental values of $\rho, u$ and $n_{\mathrm{D}}$, the internal pressure $\left(\pi_{\mathrm{i}}\right)$, free volume $\left(V_{\mathrm{f}}\right)$ and the excess functions; excess internal pressure ( $\pi_{i}^{\mathrm{E}}$ ), excess free volume ( $V_{\mathrm{f}}^{\mathrm{E}}$ ), excess enthalpy ( $H^{\mathrm{E}}$ ), excess entropy
$\left(T S^{\mathrm{E}}\right)$, excess Gibbs free energy $\left(G^{\mathrm{E}}\right)$ and deviations in refractive index ( $\Delta_{\phi} n_{D}$ ) have been calculated. The variations of these excess properties with composition indicate that the interactions between $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]$ and $\alpha, \omega$-propanediols in these mixtures follows the order: 1,2-propanediol $>1,3$-propanediol. The refractive index data are well correlated by various mixing rules.

## Supplementary Data

Supplementary data associated with this article, viz., Tables S1-S3, are available in the electronic form at http://www.niscair.res.in/jinfo/ijca/IJCA_55A(06)664 -675_SupplData.pdf.

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[^0]:    Table 1-The values of $\rho, u, n, \pi_{i}$ and $V_{\mathrm{f}}$, for the binary mixtures of [Bmim][ $\left.\mathrm{BF}_{4}\right]+1,2$-propanediol/1,3-propaqnediol as a function of mole fraction, $x_{1}$, of $[\mathrm{Bmim}]\left[\mathrm{BF}_{4}\right]$ at temperatures $\mathrm{T}=(298.15-318.15) \mathrm{K}$

