Structural analysis and theoretical investigations in Pb additive Se-Te-Ge chalcogenide nano-composites

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In the present study, the impact of lead addition on the structural and physical properties of newly prepared quaternary \((\text{Se}_{80}\text{Te}_{20})_{94-x}\text{Ge}_6\text{Pb}_x\) \((x=0, 2, 4, 6, 8 \text{ and } 10)\) chalcogenide nano–composites has been studied in detail. Nano particle size of each Pb additive chalcogenide alloy has been deduced using the highest intensity peak of the X-ray diffractograms and it has also been confirmed by field emission scanning electron microscope (FESEM). The detailed study of physical parameters namely average co-ordination number \((Z)\) and number of constraints, lone pair electrons, glass transition temperature, heat of atomization, cohesive energy and energy gap has been made. It is observed that \(Z\) and constraints have been found to increase with the addition in Pb content. However, all the other investigated parameters viz lone pair electrons, glass transition temperature, heat of atomization, cohesive energy and energy gap show a reverse variation. Glass transition temperature has been estimated theoretically using Tichy-Ticha approach and found to be in consonance with the experimental results. The cohesive energy has been calculated using chemical bond approach (CBA) model. Due to lower band gap of Pb, the overall bandgap of the composition has been found to decrease with Pb at.wt.%.

Keywords: Chalcogenide nano-composites, Glass transition temperature, Heat of atomization, Mean bond energy, Cohesive energy, Energy gap

1 Introduction

Chalcogenide nano-particles show dramatic changes in their structural, optical and electrical characteristics due to their size dependent properties. It also provides new physical and chemical properties with their applications in optical recording, optical imaging and microelectronics. Formation of nanostructure in chalcogenides becomes an interesting topic and studies in this field are still at the starting point as all the features have not been brought to the light. So there is a lot of scope for the study of these materials in a nanometric range1-4.

Se-Te based systems are preferred because they have greater hardness, higher crystallization temperature, higher photosensitivity and smaller ageing effects. Also Se-Te alloys improve the corrosion resistance and optical sensitivity5. Addition of Ge as third element to the Se-Te system increases the contribution to long term room temperature and degree of cross-linking. It is known that binary and ternary chalcogenides have some drawbacks. In the present system, we have chosen Pb as an additive element as lead chalcogenide is the only basic material of modern infrared optoelectronics. Addition of lead metallic elemental impurities to the bulk Se-Te-Ge system increases the conductivity and can also cause \(p\) to \(n\)-type transition. Pb atom is heavy due to which it provides compactness to the system. Now day’s attention is extended over quaternary systems for optoelectronic applications6-9.

In the present work, newly formulated quaternary \((\text{Se}_{80}\text{Te}_{20})_{94-x}\text{Ge}_6\text{Pb}_x\) \((x=0, 2, 4, 6, 8 \text{ and } 10)\) chalcogenide nano-composites were prepared using melt-quench technique. The structural characteristics, i.e., nano-particle size were derived using X-ray diffraction (XRD) and field emission scanning electron microscope (FESEM). The physical parameters namely average coordination number, lone pair electrons, number of constraints, fraction of floppy modes, glass transition temperature, heat of atomization, mean bond energy, energy gap and cohesive energy were deduced using different approaches and their composition dependence was discussed in detail.

2 Experimental Details

The bulk \((\text{Se}_{80}\text{Te}_{20})_{94-x}\text{Ge}_6\text{Pb}_x\) \((x=0, 2, 4, 6, 8 \text{ and } 10)\) chalcogenide alloys were prepared using melt
quenching technique. 5N highly pure materials (99.999%) were weighed according to their atomic percentages with an accuracy of 10⁻⁴ g and sealed in a quartz ampoule under a vacuum of ~10⁻⁵ torr. The sealed ampoules were then placed in a furnace for 10 h, where the temperature was raised up to 1000 °C to make the melt homogeneous. The quenching was done in the ice cold water rapidly. Structural characterization was done using XRD technique and FESEM. For these characterizations, bulk sample of the investigated composition was crushed into a very fine powder. XRD analysis was carried out with the help of Analytical X'Pert-Pro diffractometer (PW 3050/60) in the range 10°<2θ<90° at a scanning rate of 1°/min equipped with a nickel filter using Cu target source (λ = 1.5483 Å). Figure 1 shows the XRD pattern of all the investigated alloys. The XRD spectrum of (Se₈₀Te₂₀)₉₄Ge₆ confirms the amorphous nature of the ternary parent alloy as no prominent peak was observed. However, the XRD spectra of Pb additive quaternary (Se₈₀Te₂₀)₉₄₋ₓGe₆Pbₓ (x = 2, 4, 6, 8 and 10) alloys were found to associate with sharp peaks. The average particle size (D) was deduced from the highest peak intensity in the spectrum by using the Scherrer formula:

\[ D = \frac{K\lambda}{\beta \theta} \]  

where \( K \) is the Scherrer constant (\( K = 0.9 \)), \( \lambda \) is the wavelength (1.5483 Å), \( \beta \) is the full width at half the maximum (FWHM) in radiation of x-ray diffraction peak and \( \theta \) is the Bragg's angle (degree) at peak position. It was observed that the crystalline size of all the investigated Pb additive chalcogenide bulk alloys lie in nano range between 20 and 80 nm (Table 1). However, other sharp characteristic peaks (with less intensity than the highest intense peak) were also observed with the addition of Pb to the parent alloy. Thus, Pb might be compensating disorder of lower concentrations. Since reduction in disorder always leads to most stable state, as a result, the resulting composition is more stable\(^{10}\). The deduced range of the average nano range particle size of the quaternary bulk alloys was further confirmed by FESEM. FESEM correlates the surface appearance with surface morphology. It also characterizes the size and also analyses the defects. Figure 2 shows the surface morphology for investigated quaternary (Se₈₀Te₂₀)₉₄₋ₓGe₆Pbₓ (x = 0, 2, 4, 6, 8 and 10) alloys using FESEM.

The thermal behaviour of these studied nano-composites was investigated using differential scanning calorimetry (DSC) technique. About 3-5 mg of sample in powder form was encased in the aluminium pan and values of different characteristics; glass transition temperature, crystallization temperature and melting...
3 Results and Discussion

3.1 Average co-ordination number and constraints

The average co-ordination number has an immense importance in determining the structure and strength of the material. The average co-ordination number for the quaternary $\text{Se}_\alpha \text{Te}_\beta \text{Ge}_\gamma \text{Pb}_\delta$ system is given by:

$$Z = \frac{\alpha Z_{\text{Se}} + \beta Z_{\text{Te}} + \gamma Z_{\text{Ge}} + \delta Z_{\text{Pb}}}{\alpha + \beta + \gamma + \delta} \quad \ldots (2)$$

where $\alpha$, $\beta$, $\gamma$ and $\delta$ are the atomic % of Se, Te, Ge and Pb, respectively, and $Z_{\text{Se}} = 2$, $Z_{\text{Te}} = 2$, $Z_{\text{Ge}} = 4$ and $Z_{\text{Pb}} = 4$ are their respective coordination numbers. The deduced values of the average co-ordination number are given in Table 1. Figure 3 shows the variation of $Z$ with Pb at.wt.% and is found to increase with the increase in Pb content. The increase in $Z$ is attributed to the increase in the degree of cross-linking, network rigidity, strength and density between the atoms. The addition of four-fold coordinated lead atom to the two-fold coordinated Se atom increases the mean coordination number.

According to Thrope\textsuperscript{12}, for mean coordination number $<2.4$, the system is under coordinated (floppy) whereas for mean coordination number $>2.4$, network is over constrained (rigid). The floppy to rigid transformation takes place at mean coordination number $Z = 2.4$. In present study, $Z < 2.4$ for all the investigated alloys indicates that the system is floppy type. Moreover, Phillips-Thorpe approach is based on comparing the number of atomic degrees of freedom ($N_d$) with the number of interatomic force field constraints ($N_c$) indicates that if $N_d < N_c$, the network becomes over constrained and stressed-rigid.

Fig. 2 — FESEM micrographs of $(\text{Se}_{80}\text{Te}_{20})_{1-x}\text{Ge}_x\text{Pb}_x$ ($x = 0, 2, 4, 6, 8 \text{ and } 10$) nano-composites showing the surface morphology.
structures will percolate through the entire network. If \( N_d > N_c \), the network is floppy type. Thus, glass forming tendency would be maximum when number of constraints is equal to the number of degrees of freedom and no stress is present in the system \( (N_d = N_c) \). There are two types of near-neighbour bonding forces in covalent solids\(^{13}\); the bond-stretching \( (N_a = Z/2) \) and the bond-bending \( (N_b = 2Z - 3) \). The bond-bending constraints come due to angular forces and the bond-stretching constraints are due to radial forces. Therefore, the total numbers of constraints are given by:

\[
N_c = N_a + N_b \quad \ldots (3)
\]

The deduced values of \( N_c \) are given in Table 1 and are found to increase with increasing Pb content. Figure 3 indicates that number of constraints acting on the network is balanced by the number of degrees of freedom available from the atoms in the network. This implies that the increase of Pb to the system makes it more rigid.

3.2 Deviation from the stoichiometry

The parameter stoichiometry \( (R) \) determines the deviation from stoichiometry and is defined as the ratio of covalent bond possibilities of chalcogen atoms to that of non-chalcogen atoms. The analysis of \( R \) for any chalcogenide system indicates that\(^{14}\):

(i) For \( R > 1 \), the system is chalcogen rich, i.e., only heteropolar bonds and chalcogen-chalcogen bonds are present.
(ii) For \( R < 1 \), the system is chalcogen poor and only heteropolar bonds and metal-metal bonds are present.

(iii) For \( R = 1 \), the system reaches the stoichiometric composition since this is a point of existence of only heteropolar bonds.

For the present chalcogen rich system, the quantity \( R \) is deduced using the following expression:

\[
R = (aZ_{Se} + \beta Z_{Te})/(\gamma Z_{Ge} + \delta Z_{Pb}) \quad \ldots (4)
\]

The calculated values of \( R \) for each composition are listed in Table 1 and its variation with Pb at wt.% is shown in Fig. 3. The obtained values of \( R \) are greater than one \( (R > 1) \) confirms that the system under investigation is chalcogen rich.

3.3 Role of lone pair electrons in glass forming ability

Two types of interatomic forces occurred in chalcogenide glassy alloys; forces due to short range bonding interactions and forces due to interaction between lone pair electrons. The first one is explained by valence force field whereas the second one needs special contemplation. For shorter distances, the interatomic forces are repulsive. Every chalcogen has a lone pair of electrons. The repulsive lone pair electrons caused steric hurdle and also used to explain the distance of minimum approach. For larger distances, the force is attractive and is accountable for the formation of chalcogenide glasses. The number of lone pair electrons is calculated by using the model proposed by Phillips\(^{15}\):

\[
L = V - Z \quad \ldots (5)
\]

where \( V \) and \( Z \) are the valance electrons and average co-ordination number, respectively. Zhenhua suggested a criterion for binary and ternary system\(^{16}\). For binary system, the number of lone pair electrons must be greater than 2.6 while for the ternary system; it must be greater than 1. For the present investigated system, the number of lone pair electrons goes on decreasing with increasing Pb content and calculated values are given in Table 1. This is due to the interaction between the Pb ion and lone pair electrons of the bridging Se atom. The system with large number of lone pair electrons represents a stable state, specified by flexibility and will favor the glass formation by reducing the strain energy. Figure 3 shows the variation of \( L \) with Pb at wt.%

3.4 Fraction of floppy modes

The fraction of floppy modes is linked with average co-ordination number \( Z \) by the relation:

\[
f = 2 - 5Z/6 \quad \ldots (6)
\]
According to Thorpe\textsuperscript{12}, the system should contain $Z < 2.4$ for floppy mode and $Z > 2.4$ for rigid regions in the range of the glass-forming composition. According to Phillips and Thorpe\textsuperscript{15}, the best suitable condition for glass formation is when $N_c = N_d$. The values of fraction of floppy modes are given in Table 1 and it is clear that fraction of floppy modes decrease with the increase in average co-ordination number. It shows that with the increase in Pb content, the system shifted towards more rigidity as discussed earlier.

### 3.5 Mean bond energy and glass transition temperature

Mean bond energy $<E>$ is an important factor which depends upon many factors, i.e., average co-ordination number, degree of cross-linking, type of bonds and bond energy of the system. According to Tichy-Ticha\textsuperscript{17}, the mean bond energy for the chalcogen rich system is given by:

$$<E> = E_c + E_{rm} \quad \ldots (7)$$

where $E_c$ is the overall contribution to the bond energy arising from strong heteropolar bonds and is given by:

$$E_c = P_r D_{hb} \quad \ldots (8)$$

$P_r$ and $D_{hb}$ is the degree of cross-linking and average heteropolar bond energy, respectively.

$E_{rm}$ is the average bond energy per atom of the remaining matrix and is given as:

$$E_{rm} = (2[0.5Z - P_r]E_{Se-Se})/Z \quad \ldots (9)$$

where $E_{Se-Se}$ is the homopolar bond energy of Se-Se atoms. The glass transition temperature for chalcogenide glasses is an important parameter to decide their utility for the specific technological applications\textsuperscript{18}. As stated by Tichy-Ticha\textsuperscript{19}, glass transition temperature ($T_g$) is related to the mean bond energy and is given by:

$$T_g = 311 [<E> - 0.9] \quad \ldots (10)$$

where $T_g$ is in kelvin and $<E>$ is in eV/atom. The mean bond energy values have been used for the prediction of glass transition temperature as $T_g$ is directly proportional to $<E>$. Figure 4 shows the DSC thermo grams at heating rate 10 °C/min. The variation of glass transition temperature and mean bond energy in accordance with the variation of lead percentages have been plotted in Fig. 5 and found that both the factors decrease with the increase in lead. The theoretically estimated $T_g$ using Tichy-Ticha approach and experimental values from DSC data are given in Table 2 and we found that they are in consonance with each other.

**Table 2**

<table>
<thead>
<tr>
<th>Pb at. wt.%</th>
<th>$E_g$ (eV)</th>
<th>$T_g$ (K)</th>
<th>$H_s/Z$ (K/mol)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>3.0</td>
<td>550</td>
<td>2.0</td>
</tr>
<tr>
<td>2</td>
<td>2.5</td>
<td>540</td>
<td>1.7</td>
</tr>
<tr>
<td>4</td>
<td>2.0</td>
<td>530</td>
<td>1.4</td>
</tr>
<tr>
<td>6</td>
<td>1.5</td>
<td>520</td>
<td>1.1</td>
</tr>
</tbody>
</table>

Fig. 4 — DSC thermogram of the (Se\textsubscript{80}Te\textsubscript{20})\textsubscript{100-x}Ge\textsubscript{x}Pb\textsubscript{x} (x = 0, 2, 4 and 6) composition at heating rate of 10 °C/min.

Fig. 5 — Variation of $<E>$, $E_g$ and $CE$, $T_g$, $H_s/Z$ (inset) with Pb at. wt. %.
3.6 Heat of atomization, cohesive energy and energy gap

Heat of atomization \( H_s \) measures the relative bond strength. For the present investigated system heat of atomization is given by Eq. (11):

\[
H_s = (\alpha H_s^{Se} + \beta H_s^{Te} + \gamma H_s^{Ge} + \delta H_s^{Pb}) / (\alpha + \beta + \gamma + \delta) \quad \ldots (11)
\]

The heat of atomization \( (H_s) \) value for Se, Te, Ge and Pb are 227 kJ/mol, 197 kJ/mol, 377 kJ/mol and 195 kJ/mol, respectively.20 The calculated values of heat of atomization \( (H_s) \) and average single bond energy \( (H_s/Z) \) are given in Table 2. It is observed that \( H_s \) and \( H_s/Z \) decrease with the increase in Pb content. Average single bond energy \( (H_s/Z) \) measures the cohesive energy. The decrease in average bond energy also causes a decrease in the band gap. This is due to increase in the number of Se-Pb bonds (31.47 kcal/mol) and decrease in the Se-Ge bonds (49.42 kcal/mol) with the addition of Pb. Also the heat of atomization value of lead (Pb) is less than that of Ge and hence the final heat of atomization of the system decreases. This decrease in the average single bond energy with the increase in lead content may also cause the decrease in energy band gap. Bond energy of heteropolar bonds can be calculated by using the following equation suggested by Pauling:

\[
E_{A-B} = \sqrt{E_A-A \cdot E_B-B} + 30 (\chi_A - \chi_B)^2 \quad \ldots (12)
\]

where \( E_{A-B} \) is the bond energy of heteropolar bonds and \( E_A-A, E_B-B \) are the bond energies of homopolar bonds. \( \chi_A \) and \( \chi_B \) are the electronegativities of A and B elements, respectively. According to chemical bond approach (CBA), heteropolar bonds form more easily than the homopolar bonds. The different possible homopolar bonds formed in the composition are: Se-Se = 44 kcal/mol, Te-Te = 33 kcal/mol, Ge-Ge = 37.60 kcal/mol and Pb-Pb = 20.48 kcal/mol. The electronegativity values for Se, Te, Ge and Pb according to the Pauling scale are 2.55, 2.10, 2.01 and 2.33, respectively.21 Consequently, using Eq. (12), the bond strength of heteropolar bonds is: Se-Te=44.18 kcal/mol, Se-Ge=49.42 kcal/mol and Se-Pb=31.47 kcal/mol. The bond formation takes place according to decrease in their bond energies. The chemical bond distribution of possible bonds is given in Table 3. Se-Ge bonds take place firstly which are accompanied by Se-Te bonds, then Se-Pb bonds and hence lastly homopolar Se-Se bonds are formed.

Cohesive energy is the energy required to break all the bonds associated with the constituent atoms. The chemical bond approach (CBA) is used to calculate the cohesive energy of the investigated material.22 Cohesive energy is calculated by adding the bond energies of all the expected bonds in the material:

\[
CE = \sum C_i E_i \quad \ldots (13)
\]

where \( C_i \) and \( E_i \) are the number of expected chemical bonds and energy of each corresponding bond, respectively. Cohesive energy is the stabilization energy of the immense bunch of material per atom. Calculated values of \( CE \) along with the distribution of chemical bonds and energy gap values are given in Table 3. Cohesive energy of the composition

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**Table 2** — Values of mean bond energy, heat of atomization, average single bond energy, glass transition temperature for \((\text{Se}_{80}\text{Te}_{20})_{94-x}\text{Ge}_x\text{Pb}_x\) \((x = 0, 2, 4, 6, 8 \text{ and } 10)\).

<table>
<thead>
<tr>
<th>Composition</th>
<th>(&lt;E&gt;) (eV/atom)</th>
<th>(H_s) (kJ/mol)</th>
<th>(H_s/Z)</th>
<th>(T_g) (K)</th>
</tr>
</thead>
<tbody>
<tr>
<td>((\text{Se}<em>{80}\text{Te}</em>{20})_{94}\text{Ge}_6)</td>
<td>2.016</td>
<td>230.36</td>
<td>108.66</td>
<td>347.07</td>
</tr>
<tr>
<td>((\text{Se}<em>{80}\text{Te}</em>{20})_{92}\text{Ge}_6\text{Pb}_2)</td>
<td>2.004</td>
<td>229.84</td>
<td>106.40</td>
<td>343.34</td>
</tr>
<tr>
<td>((\text{Se}<em>{80}\text{Te}</em>{20})_{90}\text{Ge}_6\text{Pb}_4)</td>
<td>1.995</td>
<td>229.32</td>
<td>104.23</td>
<td>341.45</td>
</tr>
<tr>
<td>((\text{Se}<em>{80}\text{Te}</em>{20})_{88}\text{Ge}_6\text{Pb}_6)</td>
<td>1.990</td>
<td>228.80</td>
<td>102.14</td>
<td>340.00</td>
</tr>
<tr>
<td>((\text{Se}<em>{80}\text{Te}</em>{20})_{86}\text{Ge}_6\text{Pb}_8)</td>
<td>1.989</td>
<td>228.28</td>
<td>100.12</td>
<td>339.17</td>
</tr>
<tr>
<td>((\text{Se}<em>{80}\text{Te}</em>{20})_{84}\text{Ge}<em>6\text{Pb}</em>{10})</td>
<td>1.988</td>
<td>227.76</td>
<td>98.17</td>
<td>338.36</td>
</tr>
</tbody>
</table>

**Table 3** — Possible dispersal of bonds, cohesive energy and \(E_g\) for \((\text{Se}_{80}\text{Te}_{20})_{94-x}\text{Ge}_x\text{Pb}_x\) \((x = 0, 2, 4, 6, 8 \text{ and } 10)\).

<table>
<thead>
<tr>
<th>Composition</th>
<th>Possible dispersal of bonds</th>
<th>CE (kcal/mol)</th>
<th>(E_g) (eV)</th>
</tr>
</thead>
<tbody>
<tr>
<td>((\text{Se}<em>{80}\text{Te}</em>{20})_{94}\text{Ge}_6)</td>
<td>Se-Se</td>
<td>45.00</td>
<td>1.58</td>
</tr>
<tr>
<td>((\text{Se}<em>{80}\text{Te}</em>{20})_{92}\text{Ge}_6\text{Pb}_2)</td>
<td>Se-Se</td>
<td>44.24</td>
<td>1.55</td>
</tr>
<tr>
<td>((\text{Se}<em>{80}\text{Te}</em>{20})_{90}\text{Ge}_6\text{Pb}_4)</td>
<td>Se-Se</td>
<td>43.55</td>
<td>1.52</td>
</tr>
<tr>
<td>((\text{Se}<em>{80}\text{Te}</em>{20})_{88}\text{Ge}_6\text{Pb}_6)</td>
<td>Se-Se</td>
<td>42.83</td>
<td>1.49</td>
</tr>
<tr>
<td>((\text{Se}<em>{80}\text{Te}</em>{20})_{86}\text{Ge}_6\text{Pb}_8)</td>
<td>Se-Se</td>
<td>42.08</td>
<td>1.46</td>
</tr>
<tr>
<td>((\text{Se}<em>{80}\text{Te}</em>{20})_{84}\text{Ge}<em>6\text{Pb}</em>{10})</td>
<td>Se-Se</td>
<td>41.28</td>
<td>1.43</td>
</tr>
</tbody>
</table>
decreases with Pb content. This may be attributed to the replacement of stronger Se–Ge bonds (49.42 kcal/mol) by the weaker Pb–Se bonds (31.47 kcal/mol). Moreover the bond formations with lead are slightly ionic in nature and provide ionic character to the material. This weakens the network and makes the structure delicate.

The energy gap values for \((\text{Se}_{80}\text{Te}_{20})_{0.4-x}\text{Ge}_x\text{Pb}_x\) \((x = 0, 2, 4, 6, 8 \text{ and } 10)\) nano-composites are calculated theoretically\(^{22}\) using the band gap values for individual atom in the composition as Se = 1.95 eV, Te = 0.335 eV, Ge = 0.95 eV and Pb = 0 eV. The decrease in cohesive energy decreases the energy of conduction band edge that causes a decrease in the decrease in cohesive energy decreases the energy of \(T_g\) for Pb value is less as compare to the heat of atomization for Se, Te and Ge. So there is a decrease in the overall value of heat of atomization and hence average single bond energy also decreases. There is decrease in energy gap with Pb amount, which can be correlated to the decrease in average single bond energy and it can also be linked to the decrease in overall bond energies. The decrease in energy gap may also be associated with the decrease in cohesive energy.

4 Conclusions

In the present study, the structural characterization and the different physical properties viz average co-ordination number, number of constraints, lone pair electrons, fraction of floppy modes, heat of atomization, cohesive energy, mean bond energy, glass transition temperature and energy band gap are deduced for new quaternary \((\text{Se}_{80}\text{Te}_{20})_{0.4-x}\text{Ge}_x\text{Pb}_x\) \((x = 0, 2, 4, 6, 8 \text{ and } 10)\) chalcogenide nano-composites. Nano particle size of Pb additive Se-Te-Ge alloys was deduced using the XRD and is further confirmed by FESEM. Addition of Pb content to the Se-Te-Ge system increases the average co-ordination number and number of constraints, whereas, all the other investigated parameters show a reverse trend. Cohesive energy is calculated by using the CBA model and is found to decrease with the increase in Pb content. Glass transition temperature is deduced theoretically by using Tichy-Ticha approach and is found to be in concordance with the experimental values.

References